1	/16
2	/18
3	/18
4	/16
5	/19
6	/13

MASSACHUSETTS INSTITUTE OF TECHNOLOGY DEPARTMENT OF ELECTRICAL ENGINEERING AND COMPUTER SCIENCE

6.191 Computation Structures Fall 2024

Quiz #3

Name		Athena logi	n name	Score
Recitation section □ WF 10, 34-301 (Varun) □ WF 11, 34-301 (Varun) □ WF 12, 34-302 (Keshav) □ WF 1, 34-302 (Keshav)	□ WF 2, 34-303 □ WF 3, 34-303 □ WF 10, 34-302 □ WF 11, 34-302	(Pleng) (Pleng) 2 (Hilary) 2 (Hilary)	□ WF 12 □ WF 1 □ WF 2 □ WF 3 □ opt-ou	2, 34-303 (Ezra) , 34-303 (Ezra) , 34-302 (Jessica) , 34-302 (Jessica) it

Please enter your name, Athena login name, and recitation section above. Enter your answers in the spaces provided below. Show your work for potential partial credit. You can use the extra white space and the back of each page for scratch work.

Problem 1. Operating Systems (16 points)

Consider the following two processes, A and B, running on a standard RISC-V processor. Code listings use virtual addresses.

Program for process A	Program for process B
. = 0x10 .ascii "Process A: 1\n" . = 0x150 .ascii "Process A: 2\n"	. = 0x0 .ascii "Process B: 1\n" . = 0x200 .ascii "Process B: 2\n"
<pre>. = 0x200 loopA: li a0, 0x10 li a7, 0x1B ecall li a0, 0x150 li a7, 0x1B ecall j loopA</pre>	<pre>. = 0x600 loopB: li a0, 0x0 li a7, 0x1B ecall li a0, 0x200 li a7, 0x1B ecall li t0, 0x790 sw a0, 0(t0) i loopP</pre>

These processes run on a custom OS that supports segmentation-based (base and bound) virtual memory, timer interrupts for scheduling processes, and a print_string system call for printing strings.

Processes invoke syscalls with the ecall instruction. The print_string system call takes the address of a string to print as the argument in register a0, and syscall number 0x1B in register a7. It returns the length of the string that was printed. Note that the length of all of the strings is 13.

Assume virtual addresses are translated with the following base and bound registers: Process A: **base register = 0x100, bound register = 0x180** Process B: **base register = 0x700, bound register = 0x1000**

(A) (2 points) What is the physical address of the start of the string located at 0x10 in Process A and the start of the string located at 0x200 in Process B?

Physical Address of string at 0x10 in Process A:

Physical Address of string at 0x200 in Process B:

(B) (3 points) While running the two processes, you notice that one of the processes crashes due to a segmentation fault.

Which process has a segmentation fault? Circle one: Process A / Process B

Which instruction causes the segmentation fault?

- (C) (2 points) Assume that all segmentation faults have been fixed. You decide to test only Process A first to see if it behaves as expected, and get the following incorrect output, where "Process A: 1" is printed repeatedly.
 - Process A: 1 Process A: 1 Process A: 1

You isolate the issue to the handling of the exception specified by the *mcause* register. What bug in the code that handles this exception is causing the incorrect behavior?

(D) (3 points) Assume that all issues have been fixed and the processes behave as expected. Say that Process A was scheduled first, and runs until the first ecall instruction completes and returns from the common handler. What are the values in the a0, a7, and pc (in virtual address) registers? Write CAN'T TELL if you can't tell a value from the information given.

a0: _	
a7: _	
pc: _	
Process that OS returns control to after the ecall:	

- (E) (3 points) Still assume that all issues have been fixed. You run both processes and get the following output:
 - Process A: 1 Process B: 1 Process B: 2 Process A: 2

You pause the program immediately after the last line finishes printing and returns from the common handler. What are the values in the a0, t0, and pc (in virtual address) registers? Write CAN'T TELL if you can't tell a value from the information given.

a0: ₋	 	<u></u>
t0:	 	
рс: ₋	 	

(F) (3 points) Still assume that all issues have been fixed. Process A and B are now run until 4 lines are printed. For the following outputs, specify if that output could have been produced by our programs or not.

Outputs:

Process B: 1 Process A: 1 Process B: 2 Process B: 1	Process A: 1 Process A: 2 Process A: 1 Process B: 1	Process A: 1 Process B: 2 Process B: 1 Process A: 2
Circle One:	Circle One:	Circle One:
Possible / Not Possible	Possible / Not Possible	Possible / Not Possible

Problem 2. Virtual Memory (18 points)

Consider a RISC-V processor that has 16-bit virtual addresses, 2^{20} bytes of physical memory, and uses a page size of 2^{12} bytes.

(A) (2 points) Calculate the following parameters relating to the size of the page table assuming a single-level (flat) page table. Each page table entry contains a physical page number, a dirty bit, and a resident bit. *Your final answer can be a product or exponent*.

Number of entries in the page table: _____

Size of page table entry (in bits): _____

Size of the page table (in bits): _____

(B) (1 point) Instead of using a page size of 2¹² bytes, say we decide to use a page size of 2⁸ bytes. What is the ratio of the **page table sizes** with the new page size of 2⁸ bytes, compared to the old page size of 2¹² bytes? *Your final answer can use fractions, products, and exponents.*

Ratio of page table sizes: _____

For the rest of the problem, keep the **page size as 2¹² bytes**, and assume a **hierarchical page table structure of 2 levels**, with address mapping as shown below:

V	Page Offset	
1 st level index	2 nd level index	Page Offset

It is given to you that the number of bits in the 1st and 2nd level indices are equal.

(C) (2 points) Calculate the following parameters relating to the size of each second-level page table. Each second-level page table entry contains a physical page number, a dirty bit, and a resident bit. *Your final answer can be a product or exponent.*

Number of entries in each 2nd level page table: _____

Size of 2nd level page table entry (in bits): _____

(D) (8 points) You now run a test program on this processor. Execution of this test program is halted just before executing the following two instructions. The state of the hierarchical page table is shown below; the least recently used page ("LRU") and next least recently used page ("next LRU") are indicated where necessary. x1 has been set to 0x9000. Assume all physical pages are in use. Execution resumes and the following two instructions are executed:

```
. = 0xBFFC
lw x12, 0xF(x0)
sw x12, 0x0(x1) // x1 = 0x9000
```



For each virtual address accessed, please indicate, in the chart below, the virtual address, the VPN, whether the access results in a page fault, the PPN, and the physical address. *If there is not enough information given to determine a given value, please write* N/A. Please write all numerical values in hexadecimal. Assume that we use an LRU replacement policy on the 2^{nd} level of Page Tables.

Virtual Address	VPN	Page Fault (Yes/No)	PPN	Physical Address

(E) (2 points) Also, specify which PPN(s) were evicted, and which were written back to memory during execution of the two instructions from part (D). If there are no pages to list, then enter NONE.

Evicted PPN(s) (hex):

Written back PPN(s) (hex): _____

(F) (3 points) Consider the same RISC-V processor. We add a 4-element, fully-associative Translation Lookaside Buffer (TLB) with an LRU replacement policy. A program running on the processor is halted right before executing the following instruction located at address 0xB2A0. x4 has been set to 0x9204:

. = 0xB2A0 sw x3, 4(x4) // x4 = 0x9204

The contents of the TLB and the hierarchical page table are shown below. Assume that all physical pages are currently in use. Assume that we use an LRU replacement policy on the 2^{nd} level of Page Tables.



Fill out the updated state of the TLB after these operations. You may mark a row as "NO CHANGE" if it remains unchanged. Please write all numerical values in hexadecimal.

	TLB						
VPN	V	R	D	PPN			

Problem 3. Exceptions (18 points)

We are trying to run the following piece of code. Unfortunately, our processor does not implement the divide instruction. Instead, we choose to emulate the instruction within the operating system.

```
= 0 \times 000
      addi a0, x0, 0x1
      addi a1, x0, 0x1
      bnez a1, second
first:
      div a2, a1, a0
      addi a3, x0, 0x1
second:
      div a2, a1, a0
      add x0, x0, x0
      add x0, x0, x0
      add x0, x0, x0
      •••
// Kernel space
common_handler:
      csrw mscratch, x1
      lw x1, curProc
      sw x2, 0x8(x1)
      sw x3, 0xc(x1)
      sw x4, 0x10(x1)
      sw x5, 0x14(x1)
      sw x6, 0x18(x1)
     ••••
```

Note that the division instruction exception is detected in the decode stage.

(A) (4 points) Fill in all the white boxes in the 5-stage pipeline diagram for the execution of this code. Assume branches are resolved in the execute stage, and there is full bypassing. Assume that exceptions are handled lazily (at the commit point). You do not need to include bypassing arrows.

Cycle	0	1	2	3	4	5	6	7	8	9
IF										
DEC										
EXE										
MEM										
WB										

Cycle	0	1	2	3	4	5	6	7	8	9
IF										
DEC										
EXE										
MEM										
WB										

(B) (4 points) Fill this diagram out again, but now assume that we handle exceptions immediately, as soon as they are detected. You do not need to include bypassing arrows.

(C) (2 points) Suppose Alice is writing a program. Alice forgets about the ecall instruction and instead uses the jump instruction to call the common handler directly, instead of using the ecall.

example_program: li a0, 32 li a1, 10 li a7, SYS_SEMINIT j common_handler common_handler: // Save all the registers into the curProc data structure csrw mscratch, x1 ... // Setup the necessary registers to call the dispatcher // Call the dispatcher // Load all the registers from the curProc data structure // Return to the calling process

mret

Will this work as intended (circle one)? YES NO

Why or why not?

(D) (8 points) We are running the following piece of code. Determine which lines of code can be executing at the time each possible exception or interrupt happens. If there are fewer than 3 locations where the exception/interrupt can occur, please list out their PCs (e.g., 0x4). If there are 3 or more locations, then write "MANY PCs." If no PCs can be executing, write "NONE".

Assume:

- The page table initially has allocated one page for VPN 0x0.
- Each page is 2¹² bytes
- Page faults are handled by the OS
- None of these instructions cause a segmentation fault.
- If the process encounters a division by zero, it is immediately killed by the OS.
- Division instruction is implemented in hardware.

PC	Instruction
0x00	lui a1, 1 // a1 = 0x1000
0x04	lui a2, 5 // a2 = 0x5000
0x08	lw a4, 0x40(a1)
ОхОс	lw a5, 0x0(a1)
0x10	lw a6, 0x0(a2)
0x14	li a0, 0
0x18	li a7, SYS_PUTCHAR
0x1c	ecall
0x20	add a0, x0, x0
0x24	div a2, a2, a0

Interrupt/Exception Type	Current Executing Instructions
Page fault	
Timer interrupt	
System call	
Division by zero	
Illegal opcode	

Problem 4. Synchronized Space Shenanigans (16 points)

The Earth Space Research Organization (ESRO) has decided to launch a rocket to provide supplies to the astronauts living in the World Space Station (WSS). ESRO has equipped the rocket with five boosters.

All boosters run the same code. Each booster must complete a set of pre-launch checks. Each booster can independently run the pre-launch checks. Finally, the boosters must ignite only after *all five* boosters have completed the pre-launch checks. Each booster must call ignite for itself.

Engineers at ESRO have written the following code to help ignite the boosters:

```
Shared Memory:
int num_ready_boosters = 0;
booster_code:
    prelaunch_check()
    num_ready_boosters = num_ready_boosters + 1
```

```
if( num_ready_boosters == 5) {
```

```
ignite()
```

}

- (A)(4 points) Using the booster code given above, answer if the following conditions are possible:
 - 1. None of the boosters ever ignite.

Possible / Not Possible

2. All boosters ignite **after** all five boosters have completed the pre-launch checks **and** None of the boosters ignite **before** all five boosters have completed the pre-launch checks.

Possible / Not Possible

3. A booster ignites before all five boosters have completed the pre-launch checks.

Possible / Not Possible

4. What synchronization issue exists in the above code?

Race Condition / Deadlock / Both

```
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```

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- (B) (12 points) You notice that the above booster code can fail. To avoid a failed launch you decide to help out the ESRO engineers by correcting the booster code to meet the following requirements:
 - Each booster can run pre-launch checks concurrently with other boosters.
 - None of the boosters should ignite until all five boosters have completed pre-launch checks.
 - After all boosters have completed pre-launch checks, all boosters must ignite.
 - You can use at most 2 semaphores to complete the code, and you cannot initialize your semaphores to negative values.
 - There should be no race conditions or deadlocks in your code.
 - You should not introduce any extra constraints.
 - You may only add semaphore declaration and initialization in shared memory, and wait(sem) and signal(sem) instructions in the booster code.

Complete the code below. Notice that the ignite() function is now outside the if condition. Hint: Think carefully about how the if statement affects the semaphore values.

Shared Memory:

int num_ready_boosters = 0;

booster_code:

prelaunch_check()

```
num_ready_boosters = num_ready_boosters + 1
```

if(num_ready_boosters == 5) {

ignite()

}

Problem 5. Cache Coherence (19 points)

Ben Bitdiddle has a four-core processor system, where each core has its own cache. Ben has the option to use either a snoopy-based, write invalidate MSI or a snoopy-based, write invalidate MESI protocol, and is trying to decide which is better for optimizing the following code where S1 and S2 are semaphores initialized to 0. Assume that X and Y map to different lines of the cache.



Ben decides to first observe how MSI and MESI perform when run on a subset of the processes. He modifies proc1 to only perform 1 signal(S1) and 1 wait(S2) and then runs just Core A and Core B.

Core A runs:	Core B runs:
proc1:	proc2:
lw a1, X	wait(S1)
add a1, a1, a0	lw a1, Y
sw a1, Y	add a1, a1, a0
<pre>signal(S1)</pre>	sw a1, Y
wait(S2)	signal(S2)
lw a1, Y	
sw a1, X	

The semaphores guarantee that data accesses proceed in the following order. The table is given for your convenience and will not be graded.

Access	Shared Bus Transactions	Cache A		Cache B	
Initial state		X: I	Y: I	X: I	Y: I
A: lw a1, X		X:	Y:	X:	Y:
A: sw a1, Y		X:	Y:	X:	Y:
B: lw a1, Y		X:	Y:	X:	Y:
B: sw a1, Y		X:	Y:	X:	Y:
A: lw a1, Y		X:	Y:	X:	Y:
A: sw a1, X		X:	Y:	X:	Y:

(A) (4 points) For each protocol, how many of each of the following bus requests occur for the series of accesses listed above?

Protocol	# of BusRd	# of BusRdX	# of BusWB
MSI			
MESI			

(B) (1 point) Assuming that instructions always interleave in the same order, when switching from a MSI protocol to a MESI protocol, which of the following # of bus requests *could* decrease?

# of BusRd:	Could decrease	Stays the same
# of BusRdX:	Could decrease	Stays the same
# of BusWB:	Could decrease	Stays the same

After observing how his code performs on MSI and MESI with just 2 cores, he thinks he has enough information to decide which is better for his 4 core system.

(C) (2 points) Ben's MESI protocol takes 10ns longer than his MSI protocol per cache access. Suppose all bus transactions(BusRd, BusRdX, BusWB) take an additional 80ns if they are called. For Ben's system that has a total of 10 data accesses(1 lw X, 1 sw X, 4 lw Y, 4 sw Y), how many bus transactions need to be saved for the MESI protocol to take less total time than the MSI protocol?

Minimum number of saved bus transactions:

(D) (1 point) What is the maximum number of bus transactions that would be saved if Ben uses the MESI protocol over the MSI protocol? (Hint: pay close attention to what the semaphores guarantee about data access order)

Maximim number of saved bus transactions using Ben's code:

(E) (1 point) Should Ben use his MSI or MESI protocol (circle one)?

MSI

MESI

Core A	Core B	Core C	Core D
(1) lw a1, X (2) sw a1, Y (9) lw a1, Y (10) sw a1, X	(4) lw al, Y (5) sw al, Y	(3) lw al, Y (7) sw al, Y	(6) lw al, Y (8) sw al, Y

(F) (10 points) Suppose Ben's program interleaves data accesses in the following order:

Fill in the following table using the protocol you selected in part E (**this table WILL be graded**). Include all shared bus transactions. Include the address associated with each bus transaction (e.g., **BusRdX(Y)**). If no bus transactions occur, write N/A in the corresponding box. Cache states left blank will be assumed to be Invalid.

Access	Shared Bus Transactions	Cach	Cache A		Cache A		Cache A		Cache A C		Cache B		Cache C		Cache D	
Initial state		X: I	Y: I													
A: lw a1, X		X:	Y:	X:	Y:	X:	Y:	X:	Y:							
A: sw a1, Y		X:	Y:	X:	Y:	X:	Y:	X:	Y:							
C: lw a1, Y		X:	Y:	X:	Y:	X:	Y:	X:	Y:							
B: lw a1, Y		X:	Y:	X:	Y:	X:	Y:	X:	Y:							
B: sw a1, Y		X:	Y:	X:	Y:	X:	Y:	X:	Y:							
D: lw a1, Y		X:	Y:	X:	Y:	X:	Y:	X:	Y:							
C: sw a1, Y		X:	Y:	X:	Y:	X:	Y:	X:	Y:							
D: sw a1, Y		X:	Y:	X:	Y:	X:	Y:	X:	Y:							
A: lw a1, Y		X:	Y:	X:	Y:	X:	Y:	X:	Y:							
A: sw al, X		X:	Y:	X:	Y:	X:	Y:	X:	Y:							

Problem 6. Cache Me If You Can (13 points)

Oh no, Didit is broken! The 6.004 TAs are scrambling to put together a grading script that calculates student grades so that they can get class grades submitted before the deadline.

The student grades are stored in an array int G[S][N] such that S is the number of students in the class, N is the total number of assignments in the class and G[s][n] corresponds to the grade obtained by student number s on assignment number n.

Additionally, there's an array called int W[N] which stores the per-assignment weights. The TAs want to calculate the total score of the class in a register variable called sum. All the arrays are stored in **row-major configuration**.

(A) (2 points) A couple of TAs suggest the following two versions of the script:

Version A:	Version B:
<pre>void grade() {</pre>	<pre>void grade() {</pre>
<pre>int sum = 0;</pre>	int sum = 0;
for (int n = 0; n < N; n++)	for (int s = 0; s < S; s++)
<pre>for (int s = 0; s < S; s++)</pre>	for (int n = 0; n < N; n++)
sum += W[n] * G[s][n];	sum += W[n] * G[s][n];
}	}

Which version has better data locality? Why?

Version with better Data Locality (circle): A B

Explanation:

The program runs on a CPU with separate instruction and data caches. For this problem, assume that instructions, W, and G arrays **reside in three different caches respectively**, and we want to analyze the data misses on the W array. The W array cache is a **fully associative** cache with **4 words per block**, with **LRU eviction policy**. Assume that we run **Version B** of the code and that there are 64 students in the class (S = 64) and 16 assignments (N = 16). The table below shows the number of data misses on the W array for different cache sizes.

W Array Cache Size words (lines x words/line)	Data misses on W
12 (3 x 4)	256
16 (4 x 4)	4

Cache diagrams and code are available on the following pages for assistance and scratch work.

(B) (3 points) Why does increasing the cache size slightly have such a large improvement in the number of misses on the W array? Briefly explain.

Explanation:

(C) (4 points) Unfortunately, the TAs will be unable to get more cache in time for the deadline. Help the TAs tile Version B of the code with a tile size of T. Assume that S and N are divisible by T. Your goal is to minimize the number of misses on W, and you can only tile either S or N. Which one should you tile on? Complete the code below showing a tiled implementation of the code.

<pre>Version C: void grade() { int sum = 0;</pre>	
for ()
for ()
for ()
sum += }	

(D) (4 points) Calculate the total number of data-misses on the W array using your tiled code from part C. Assume the **tiling factor** T = 4 and that you are using the **12 word (3 x 4) cache**.

Cache diagrams and code are available on the following pages for assistance and scratch work.

Data misses on the W array: _____

W array cache diagrams for fully associative caches with <u>12 words</u>, 4 words per block (not graded):

```
Version B:
void grade() { // S = 64, N = 16
    int sum = 0;
    for (int s = 0; s < S; s++)
        for (int n = 0; n < N; n++)
            sum += W[n] * G[s][n];
}
```

Tag	Word 3		Word 3 Word		Word 2 Word 1		Word 0	
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W []
	W[]	W []	W []	W []

Extra Copies:

Tag	Word 3		Word 3		Word 3 Word 2		Word 1		Word 0	
	W[]	W[]	W[]	W[]		
	W[]	W[]	W[]	M[]		
	W[]	W[]	W[]	W []		

Tag	Word 3		Woi	rd 2	Wor	rd 1	Wor	'd 0
	W[]	W[]	W[]	M[]
	W[]	W[]	W[]	M[]
	W[]	W[]	W[]	W []

Tag	Word 3		Wor	·d 2	Wor	•d 1	Wor	rd 0
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W[]

Tag	Word 3		Wor	·d 2	Word 1		Wor	'd 0
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W []
	W []	W[]	W[]	W []

Tag	Word 3		Wor	rd 2	Wor	Word 1		'd 0
	W[]	W[]	W[]	W[]
	M[]	W[]	W[]	W []
	W[]	W[]	W[]	W[]

W array cache diagrams for fully associative caches with <u>16 words</u>, 4 words per block (not graded):

```
Version B:
void grade() { // S = 64, N = 16
    int sum = 0;
    for (int s = 0; s < S; s++)
        for (int n = 0; n < N; n++)
            sum += W[n] * G[s][n];
}
```

Tag	Word 3		Wo	rd 2	Wor	·d 1	Wor	·d 0
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W []

Extra Copies:

Tag	Word 3		Woi	Word 2		rd 1	Word 0	
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W[]

Tag	Word 3		Word 2		Word 1		Word 0	
	W[]	W[]	M[]	W[]
	W []	W[]	W[]	W []
	W[]	W[]	M[]	W[]
	W[]	W[]	W[]	W[]

Tag	Word 3		Word 2		Word 1		Word 0	
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W[]

Tag	Wo	rd 3	Woi	·d 2	Wor	·d 1	Wor	'd 0
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W[]

W array cache diagrams for fully associative caches with <u>12 words</u>, 4 words per block, and a tile size of 4. (not graded):

Tag	Word 3		Word 2		Word 1		Word 0	
	W[]	W[]	W[]	M[]
	W[]	W[]	W[]	M[]
	W[]	W[]	W[]	M[]

Extra Copies:

Tag	Word 3		Word 2		Word 1		Word 0	
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W[]

Tag	Word 3		Woi	rd 2	Wor	·d 1	Wor	·d 0
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W []

Tag	Word 3		Word 2		Word 1		Word 0	
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W []
	W[]	W[]	W[]	W []

Tag	Word 3		Word 2		Word 1		Word 0	
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W[]
	W[]	W[]	W[]	W []

END OF QUIZ 3!